Math 142 EXAM 1 REVIEW – CHAPTERS 1–2

- **1.** (1.1) What is the measure of the angle between the hands of a clock when it reads 3:40?
- **2.** (1.1) In $\triangle ABC$, $m \angle C = 90^\circ$, AB = 10 and BC = $5\sqrt{2}$. Find AC.
- **3.** (1.2) Find the distance between the points (-1, 4) and (-5, 6).
- 4. (1.2) Find one positive and one negative angle that is coterminal with 173° (answers may vary).
- 5. (1.3) Consider the angle $\theta = 120^{\circ}$
 - (a) Draw θ in the standard position on the coordinate axes.
 - (b) Find a point on the terminal side (answers may vary).
 - (c) Find $\sin \theta$, $\cos \theta$ and $\tan \theta$.
- 6. (1.3) Find $\tan \phi$ if $\sin \phi = \frac{2}{\sqrt{5}}$ and ϕ terminates in QII.
- **7.** (1.3) Find $\cos \theta$ if the terminal side of θ lies on the line $y = -\frac{1}{4}x$ in QII.
- **8.** (1.4) From memory, state allthree Pythagorean identities.
- **9.** (1.5) Simplify the expression $\sqrt{16 x^2}$ as much as possible after substituting $4\sin\phi$ for x.
- 10. (1.5) Show that the following statement is an identity by transforming the left side until it matches the right side. Be organized and do not skip steps.

$$\frac{\cos^2\theta}{\sin\theta} = \csc\theta - \sin\theta$$

11. (2.1) Consider a right triangle with one acute angle labeled θ and the appropriate sides labeled "opposite", "adjacent" and "hypotenuse." From memory, list the ratios representing all six trigonometric functions of the angle θ .

- **12.** (2.1) Without the use of a calculator, find the exact value for each of the following:
 - (a) $\sin 60^{\circ}$
 - (b) tan 30°
 - (c) $\cos 0^{\circ}$
 - (d) sec 45°
- **13.** (2.2) Subtract: $45^{\circ} 13' 22^{\circ} 32'$
- 14. (2.2) Use a calculator to approximate each of the following. Round each answer to the nearest thousandth.
 - (a) $\sin 12.5^{\circ}$
 - (b) cot 77° 29′
 - (c) $\sec 81^\circ 17' 50''$
- 15. (2.3) In $\triangle ABC$, m $\angle C = 90^\circ$, AC = 55 m and $m \angle B = 17^{\circ}$. Find AB rounded to the nearest tenth of a meter.
- 16. (2.3) In the triangle below, find the measure of angle A to the nearest minute.



17. (2.4) An icicle in the shape of a cone, measures 8 inches down the side and the angle at the tip is 20° . Find the volume of the icicle to the

nearest hundredth of a cubic inch. The formula for the volume of a cone is $V = \frac{1}{3}\pi r^2$

20°

- 18. (2.4) Two ships leave a harbor at the same time, one with a bearing of N 57° W and the other with a bearing of N 57° E, and both travel for 80 miles. What is the distance between the ships?
- 19. (2.5) A cannonball is fired with an initial velocity of 200 feet per second at an angle of 43° above horizontal. Find the magnitudes of the horizontal and vertical vector components of the velocity vector. Round your answer to one decimal place.

1. 130° 2. AC = $5\sqrt{2}$ 3. $2\sqrt{5}$ 4. 533° and -187° 5. (b) $(-1,\sqrt{3})$; (c) $\sin\theta = \frac{\sqrt{3}}{2}$, $\cos\theta = -\frac{1}{2}$, $\tan\theta = -\sqrt{3}$, 6. $\tan \phi = -2$ 7. $-\frac{4\sqrt{17}}{17}$ 8. $\cos^2 \theta + \sin^2 \theta = 1$, $\sec^2 \theta = \tan^2 \theta + 1$, $\csc^2 \theta = \cot^2 \theta + 1$ 9. $4|\cos\phi|$ 10. $\frac{\cos^2 \theta}{\sin \theta} = \frac{1 - \sin^2 \theta}{\sin \theta} = \frac{1}{\sin \theta} - \sin \theta = \csc \theta - \sin \theta$ 11. $\sin \theta = \frac{\text{opp}}{\text{hyp}}, \ \cos \theta = \frac{\text{adj}}{\text{hyp}}, \ \tan \theta = \frac{\text{opp}}{\text{adj}}, \ \csc \theta = \frac{\text{hyp}}{\text{opp}}, \ \sec \theta = \frac{\text{hyp}}{\text{adj}}, \ \cot \theta = \frac{\text{adj}}{\text{opp}},$ 12. (a) $\frac{\sqrt{3}}{2}$; (b) $\frac{\sqrt{3}}{3}$; (c) 1; (d) $\sqrt{2}$ 13. 22° 41′ 14. (a) 0.216; (b) 0.222; (c) 6.609 15. AB $\approx 188.1\,\mathrm{m}$ 16. A $\approx 39^\circ\,46'$ 17. about 15.92 in^3 18. about 134.2 miles

19. horizontal is about 146.3 ft/sec, vertical is about 136.4 ft/sec