

Calculus I Skills Review

Write the solution to each derivative from memory. For any you do not remember, make a point to memorize them before attempting new material in Calculus II.

1. $\frac{d}{dx} [x^5]$

2. $\frac{d}{dx} [\sqrt{x}]$

3. $\frac{d}{dx} \left[\frac{1}{x^4} \right]$

4. $\frac{d}{dx} [\sin x]$

5. $\frac{d}{dx} [\cos x]$

6. $\frac{d}{dx} [\tan x]$

7. $\frac{d}{dx} [\csc x]$

8. $\frac{d}{dx} [\sec x]$

9. $\frac{d}{dx} [\cot x]$

10. $\frac{d}{dx} [e^x]$

11. $\frac{d}{dx} [\ln(x)]$

12. $\frac{d}{dx} [\arcsin x]$

13. $\frac{d}{dx} [\arctan x]$

Evaluate each derivative.

14. $\frac{d}{dx} [x^3 \sin x]$

15. $\frac{d}{dx} \left[\frac{x^2}{3x^3 + 8} \right]$

16. $\frac{d}{dx} [e^{3x}]$

17. $\frac{d}{dx} [\ln(x^5 + 7)]$

18. $\frac{d}{dx} [\cos^2 x]$

19. $\frac{d}{dx} [\arcsin x^2]$

Write the solution to each integral from memory.

20. $\int x^5 dx$

21. $\int \sqrt[3]{x} dx$

22. $\int e^x dx$

23. $\int \frac{1}{x} dx$

24. $\int \frac{1}{x^2} dx$

25. $\int \frac{1}{\sqrt{x}} dx$

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26. $\int \sin x dx$

27. $\int \cos x dx$

28. $\int \sec^2 x dx$

29. $\int \csc^2 x dx$

30. $\int \sec x \tan x dx$

31. $\int \csc x \cot x dx$

32. $\int \tan x dx$

33. $\int \cot x dx$

34. $\int \sec x dx$

35. $\int \csc x dx$

Evaluate each integral using substitution.

36. $\int x \sqrt{x^2 + 36} dx$

37. $\int \frac{x^2}{x^3 - 27} dx$

38. $\int \sec^2(\pi x) dx$

39. $\int (\sin x)e^{\cos x} dx$

40. $\int \frac{1}{x^{2/3} \sqrt{x^{1/3} + 9}} dx$

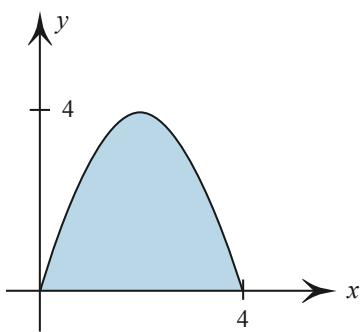
Evaluate each definite integral.

41. $\int_0^4 \sqrt{x} dx$

42. $\int_1^e \frac{\ln(x)}{x} dx$

43. $\int_1^{16} \frac{1}{\sqrt{x}(1 + \sqrt{x})^2} dx$

44. Determine the area of the shaded region shown with $y = x(4 - x)$.



Answers

1. $5x^4$ 2. $\frac{1}{2\sqrt{x}}$ 3. $-\frac{4}{x^5}$ 4. $\cos x$
5. $-\sin x$ 6. $\sec^2 x$ 7. $-\csc x \cot x$
8. $\sec x \tan x$ 9. $-\csc^2 x$ 10. e^x
11. $\frac{1}{x}$ 12. $\frac{1}{\sqrt{1-x^2}}$ 13. $\frac{1}{1+x^2}$
14. $x^2(3 \sin x + x \cos x)$ 15. $\frac{x(16 - 3x^3)}{(3x^3 + 8)^2}$
16. $3e^{3x}$ 17. $\frac{5x^4}{x^5 + 7}$ 18. $-2 \cos x \sin x$
19. $\frac{2x}{\sqrt{1-x^4}}$ 20. $\frac{x^6}{6} + C$ 21. $\frac{3\sqrt[3]{x^4}}{4} + C$
22. $e^x + C$ 23. $\ln|x| + C$ 24. $-\frac{1}{x} + C$
25. $2\sqrt{x} + C$ 26. $-\cos x + C$ 27. $\sin x + C$
28. $\tan x + C$ 29. $-\cot x + C$ 30. $\sec x + C$
31. $-\csc x + C$ 32. $-\ln|\cos x| + C$
33. $\ln|\sin x| + C$ 34. $\ln|\sec x + \tan x| + C$
35. $-\ln|\csc x + \cot x| + C$
36. $\frac{1}{3}(x^2 + 36)^{3/2} + C$
37. $\frac{1}{3}\ln|x^3 - 27| + C$ 38. $\frac{1}{\pi} \tan \pi x + C$
39. $-e^{\cos x} + C$ 40. $6\sqrt{x^{1/3} + 9} + C$
41. $\frac{16}{3}$ 42. $\frac{1}{2}$ 43. $\frac{3}{5}$ 44. $\frac{32}{3}$