



Component	Description	Unit of Measure
$q(t)$	Flow of charge	coulombs ($C = A \cdot \text{sec}$)
$i(t) = q'(t)$	Current	amperes (A)
Resistors, R	Resists flow of charge. Used to control flow. $\Delta V_R = iR$	ohms ($\Omega = V/A$)
Capacitors, C	Stores charge and opposes passage of current. Used to store voltage. $\Delta V_C = \frac{1}{C}q$	farads ($F = A \cdot \text{sec}/V$)
Inductors, L	Opposes change in current flowing through it. Used to store current. $\Delta V_L = L \frac{di}{dt}$	henrys ($H = \Omega \cdot \text{sec}$)
Electromotive force, $E(t)$	Source of voltage	volts (V)

Kirchhoff's Second Law

As a consequence of the law of conservation of energy, the sum of the voltage drops around a closed circuit is zero.

$$\Delta V_L + \Delta V_R + \Delta V_C - E(t) = 0$$

$$\implies L \frac{di}{dt} + Ri + \frac{1}{C}q = E(t)$$

1. Find an equation for the current, $i(t)$ for $t > 0$ in a circuit with resistance of 7 ohms, inductance of 5 henrys and no capacitors (an RL circuit) and an electromotive force of 70 V. Assume that the current at $t = 0$ is 2 amperes.
2. An RC circuit has a resistance of $5\ \Omega$, a capacitance of $\frac{1}{50}$ F, and an electromotive force of 100 V. If the capacitor is uncharged initially, determine the current in the circuit for $t > 0$.
3. Find the current of an RL circuit with $E(t) = 10 \sin 4t$, $R = 2\ \Omega$, $L = \frac{2}{3}$ H, and there is no current flowing initially.
4. Determine the current flowing in an RC circuit if $R = 2\ \Omega$, $C = 15$ F, the capacitor is initially uncharged and the driving EMF is given by $E(t) = Ae^{-kt}$, where A and k are constants.

1. $i(t) = 10 - 8e^{-7t/5}$

2. $i(t) = 20e^{-10t}$

3. $i(t) = \frac{3}{5}(3 \sin 4t - 4 \cos 4t) + \frac{12}{5}e^{-3t}$

4. $i(t) = \frac{15A}{1 - 30k} \left(\frac{1}{30}e^{-t/30} - ke^{-kt} \right)$